

A new experimental test of Bell inequalities by the use of a non-maximally entangled photon state

G.Brida, M.Genovese *, C.Novero

*Istituto Elettrotecnico Nazionale Galileo Ferraris, Str. delle Cacce
91, I-10135 Torino,*

E. Predazzi

Dip. Fisica Teorica Univ. Torino e INFN, via P. Giuria 1, I-10125 Torino

Abstract

We report on the realisation of a new test of Bell inequalities using the superposition of type I parametric down conversion produced in two different non-linear crystals pumped by the same laser, but with different polarisations.

We discuss the advantages and the possible developments of this configuration.

PACS: 03.65.Bz

Keywords: Bell inequalities, non-locality, hidden variable theories

Many experiments have already been devoted to a test of Bell inequalities [1–5], leading to a substantial agreement with quantum mechanics and disfavouring realistic local hidden

*genovese@ien.it. Tel. 39 011 3919234, fax 39 011 3919259

variable theories. However, due to the low total detection efficiency (the so-called "detection loophole") no experiment has yet been able to exclude definitively realistic local hidden variable theories, for it is necessary a further additional hypothesis [7], stating that the observed sample of particles pairs is a faithful subsample of the whole. This problem is known as detection or efficiency loophole. Considering the extreme relevance of a conclusive elimination of local hidden variable theories, the research for new experimental configurations able to overcome the detection loophole is of a great interest.

A very important theoretical step in this direction has been achieved recognising that for non maximally entangled pairs a total efficiency larger than 0.67 [8] (in the limit of no background) is required to obtain an efficiency-loophole free experiment, whilst for maximally entangled pairs this limit rises to 0.81. However, it must be noticed that for non-maximally entangled states the largest discrepancy between quantum mechanics and local hidden variable theories is reduced: thus a compromise between a lower total efficiency and a still sufficiently large value of this difference will be necessary in a realisation of an experiment addressed to overcome the detection loophole.

On the experimental side, in recent years the largest improvements have been obtained by using parametric down conversion (PDC) processes.

This technique has been employed, since its discovery, for generations of "entangled" photon pairs, i.e. pairs of photons described by a common wave function which by no means can be factored up into the product of two distinct wave functions pertaining to separated photons. It is due essentially to L. Mandel and collaborators [1] the idea of using such a state of the electromagnetic field to perform tests of quantum mechanics, more specifically to test Bell's inequalities.

The generation of entangled states by parametric down conversion is alternative to other techniques, such as the radiative decay of atomic excited states, as it was in the celebrated experiment of A. Aspect et al. [2], and overcomes some former limitations in the direction of propagation of the conjugated photons. In fact the poor angular correlation of atomic cascade photons is at the origin of a small total efficiency of this set up, leading to a selection

of a small subsample of the produced photons, which makes impossible to eliminate the detection loophole in this case. On the other hand, a very good angular correlation (better than 1 mrad) of the two photons of the pair is obtained in the PDC process, giving the possibility, at least in principle, to overcome the previous problem.

The entanglement on phase and momentum, which is directly produced in Type I parametric down conversion can be used for a test of Bell inequalities using two spatially separated interferometers [3], as realised by [4]. The use of beam splitters, however, strongly reduces the total quantum efficiency.

In alternative, one can generate a polarisation entangled state [6]. It appears, however, that the creation of couples of photons entangled from the point of view of polarisation, which is by far the most diffuse case due to the easy experimental implementation, still suffers severe limitations, as it was pointed out recently in the literature. The essence of the problem is that in generating this state, half of the initial photon flux is lost (in most of the used configurations), and one is, of necessity, led to assume that the photon's population actually involved in the experiment is a faithful sample of the original one, without eliminating the efficiency loophole.

A scheme which allows no postselection of the photons has been realised recently, using Type II PDC, where a polarisation entangled state is directly generated. This scheme has effectively permitted, at the price of delicate compensations for having identical arrival time of the ordinary and extraordinary photon, a much higher total efficiency than the previous ones. It is, however, still far from the value 0.81 for the total efficiency. Also, some recent experiments studying equalities among correlations functions rather than Bell inequalities [9] are far by solving these problems [10]. A large interest remains therefore for new experiments increasing total quantum efficiency in order to reduce and finally overcome the efficiency loophole.

Our experiment follows and develops [11] an idea by Hardy [12] and contemplates the creation of a polarisation (non maximally-) entangled states of the form

$$|\psi\rangle = \frac{|H\rangle|H\rangle + f|V\rangle|V\rangle}{\sqrt{(1 + |f|^2)}} \quad (1)$$

(where H and V indicate horizontal and vertical polarisations respectively) via the superposition of the spontaneous fluorescence emitted by two non-linear crystals driven by the same pumping laser. The crystals are put in cascade along the propagation direction of the pumping laser and the superposition is obtained by using an appropriate optics.

We describe more in details the experimental set-up, with reference to the sketch of figure 1 below. The two crystals of LiIO_3 (10x10x10 mm) are 250 mm apart, a distance smaller than the coherence length of the pumping laser. This guarantees indistinguishability in the creation of a couple of photons in the first or in the second crystal. A couple of planoconvex lenses of 120 mm focal length centred in between focalises the spontaneous emission from the first crystal into the second one maintaining exactly, in principle, the angular spread. A hole of 4 mm diameter is drilled into the centre of the lenses in order to allow transmission of the pump radiation without absorption and, even more important, without adding stray-light, because of fluorescence and diffusion of the UV radiation. This configuration, which performs as a so-called "optical condenser", was chosen among others as a compromise between minimisation of aberrations (mainly spherical and chromatic) and losses due to the number of optical components. The pumping beam at the exit of the first crystal is displaced from its input direction by birefringence: the small quartz plate (5 x5 x5 mm) in front of the first lens of the condensers compensates this displacement, so that the input conditions are prepared to be the same for the two crystals, apart from alignment errors. Finally, a half-wavelength plate immediately after the condenser rotates the polarisation of the Argon beam and excites in the second crystal a spontaneous emission cross-polarised with respect to the first one. The dimensions and positions of both plates are carefully chosen in order not to intersect the spontaneous emissions at 633 and 789 nm. With a phase matching angle of 51° they are emitted at 3.5° and 4° respectively.

The precise value of f , which determines how far from a maximally entangled state ($f = 1$) the produced state is, can be easily tuned by modifying the pump intensity between the two crystals. This is a fundamental property, which could permit to select the most appropriate state for the practical realisation of a detection loophole free experiment.

The alignment (which is of fundamental importance for having a high visibility and in principle constitutes the main problem of such a configuration) has been profitably improved using an optical amplifier scheme, where a solid state laser is injected into the crystals together with the pumping laser, an argon laser at 351 nm wavelength (see fig.1). Such a technique had already proved its validity and it is of great help in the recognition of the directions of propagation of correlated wavelengths photon and applied in our laboratory [13] for metrological studies.

The proposed scheme is well suited for leading to a further step toward a conclusive experimental test of non-locality in quantum mechanics. The analysis of the experiments realised up to now [7] shows in fact that visibility of the wanted effect (essentially visibility of interference fringes) and overall quantum efficiency of detection are the main parameters in such experiments. One first advantage of the proposed configuration with respect to most of the previous experimental set-ups is that all the entangled pairs are selected (and not only 50% as with beams splitters).

For the moment, the results which we are going to discuss are still far from a definitive solution of the detection loophole; nevertheless, being the first test of Bell inequalities using a non-maximally entangled state, they represents an important step in this direction. Furthermore, this configuration permits to use any pair of correlated frequencies and not only the degenerate ones. We have thus realised this test using for a first time two different wave lengths (at 633 and 789 nm).

A somehow similar set-up has been realised recently in ref. [14]. The main difference between the two experiments is that in [14] the two crystals are very thin and in contact with orthogonal optical axes: this permits a "partial" superposition of the two emissions with opposite polarisation. This overlapping is mainly due to the finite dimension of the pump laser beam, which reflects into a finite width of each wavelength emission. We think that the arrangement, described in the present paper is better, in that by fine tuning the crystals' and optics' positions a perfect superposition can be obtained for at least a couple of wavelength in PDC emission. Moreover, the parametric amplifier trick allows to approach

this ideal situation very closely. Furthermore, in the experiment of ref. [14] the value of f is in principle tunable by rotating the polarisation of the pump laser, however this reduce the power of the pump producing PDC already in the first crystal, while in our case the whole pump power can always be used in the first crystal, tuning the PDC produced in the second one.

As a first check of our apparatus, we have measured the interference fringes, varying the setting of one of the polarisers, leaving the other fixed. We have found a high visibility, $V = 0.973 \pm 0.038$.

Our results are summarised by the value obtained for the Clauser-Horne sum,

$$CH = N(\theta_1, \theta_2) - N(\theta_1, \theta'_2) + N(\theta'_1, \theta_2) + N(\theta'_1, \theta'_2) - N(\theta'_1, \infty) - N(\infty, \theta_2) \quad (2)$$

which is strictly negative for local realistic theory. In (2), $N(\theta_1, \theta_2)$ is the number of coincidences between channels 1 and 2 when the two polarisers are rotated to an angle θ_1 and θ_2 respectively (∞ denotes the absence of selection of polarisation for that channel)

For quantum mechanics CH can be larger than zero, e.g. for a maximally entangled state the largest value is obtained for $\theta_1 = 67^\circ.5$, $\theta_2 = 45^\circ$, $\theta'_1 = 22^\circ.5$, $\theta'_2 = 0^\circ$ and correspond to a ratio

$$R = [N(\theta_1, \theta_2) - N(\theta_1, \theta'_2) + N(\theta'_1, \theta_2) + N(\theta'_1, \theta'_2)] / [N(\theta'_1, \infty) + N(\infty, \theta_2)] \quad (3)$$

equal to 1.207.

For non-maximally entangled states the angles for which CH is maximal are somehow different and the largest value smaller. The angles corresponding to the maximum can be evaluated maximising Eq. 2 with

$$\begin{aligned}
N[\theta_1, \theta_2] = & [\epsilon_1^{\parallel} \epsilon_2^{\parallel} (\sin[\theta_1]^2 \cdot \sin[\theta_2]^2) + \\
& \epsilon_1^{\perp} \epsilon_2^{\perp} (\cos[\theta_1]^2 \cdot \cos[\theta_2]^2) \\
& (\epsilon_1^{\perp} \epsilon_2^{\parallel} \sin[\theta_1]^2 \cdot \cos[\theta_2]^2 + \epsilon_1^{\parallel} \epsilon_2^{\perp} \cos[\theta_1]^2 \cdot \sin[\theta_2]^2) \\
& + |f|^2 * (\epsilon_1^{\perp} \epsilon_2^{\perp} (\sin[\theta_1]^2 \cdot \sin[\theta_2]^2) + \epsilon_1^{\parallel} \epsilon_2^{\parallel} (\cos[\theta_1]^2 \cos[\theta_2]^2) + \\
& (\epsilon_1^{\parallel} \epsilon_2^{\perp} \sin[\theta_1]^2 \cdot \cos[\theta_2]^2 + \\
& \epsilon_1^{\perp} \epsilon_2^{\parallel} \cos[\theta_1]^2 \cdot \sin[\theta_2]^2) \\
& + (f + f^*)((\epsilon_1^{\parallel} \epsilon_2^{\parallel} + \epsilon_1^{\perp} \epsilon_2^{\perp} - \epsilon_1^{\parallel} \epsilon_2^{\perp} - \epsilon_1^{\perp} \epsilon_2^{\parallel}) \cdot (\sin[\theta_1] \cdot \sin[\theta_2] \cdot \cos[\theta_1] \cdot \cos[\theta_2]))] / (1 + |f|^2)
\end{aligned} \tag{4}$$

where (for the case of non-ideal polariser) ϵ_i^{\parallel} and ϵ_i^{\perp} correspond to the transmission when the polariser (on the branch i) axis is aligned or normal the polarisation axis respectively.

In our case we have a state with $f \simeq 0.4$ which corresponds, for $\theta_1 = 72^\circ.24$, $\theta_2 = 45^\circ$, $\theta'_1 = 17^\circ.76$ and $\theta'_2 = 0^\circ$, to $R = 1.16$.

Our experimental result is $CH = 512 \pm 135$ coincidences per second, which is almost four standard deviations different from zero and compatible with the theoretical value predicted by quantum mechanics. In terms of the ratio (3), our result is 1.082 ± 0.031 .

It must be noticed that results which are by far of many more standard deviations above zero have been obtained. Nevertheless, to our knowledge, this is the first measurement of the Clauser-Horne sum (or other Bell inequalities) using a non-maximally entangled state and thus represents an interesting result as a first step in the direction of eliminating the detection loophole. This is also the first measurement of a polarisation two photon entanglement state, where the two photons have different wavelengths. Further developments in this sense are the purpose of this collaboration.

Acknowledgements

We would like to acknowledge support of Italian Space Agency under contract LONO 500172.

REFERENCES

- [1] see L. Mandel, and E. Wolf, Optical Coherence and Quantum Optics, Cambridge University Press, 1995 and references therein.
- [2] A. Aspect et al., Phys. Rev. Lett. 49 , 1804, (1982).
- [3] J. P. Franson, Phys. Rev. Lett. 62, 2205 (1989).
- [4] J. G. Rarity, and P. R. Tapster, Phys. Rev. Lett. 64, 2495 (1990); J. Brendel et al. Eur.Phys.Lett. 20, 275 (1992); P. G. Kwiat et al, Phys. Rev. A 41, 2910 (1990); W. Tittel et al, quant-ph 9806043
- [5] T.E. Kiess et al., Phys. Rev. Lett. 71, 3893, (1993); P.G. Kwiat et al., Phys. Rev. Lett. 75, 4337, (1995).
- [6] Z.J. Ou and L. Mandel, Phys. Rev. Lett. 61, 50, (1988); Y.H.Shih et al., Phys. Rev. A, 1288, (1993).
- [7] E. Santos, Phys. Lett. A 212, 10 (1996); L. De Caro and A. Garuccio Phys. Rev. A 54, 174 (1996) and references therein.
- [8] P. H. Eberhard, Phys. Rev. A 47, R747 (1993).
- [9] J.R.Torgerson et al., Phys. Lett. A 204, 323 (1995); G.Di Giuseppe, F.De Martini and D.Boschi, Physical Review A 56, 176 (1997); D.Boschi, S.Branca, F.De Martini and L.Hardy, Phys. Rev. Lett. 79, 2755 (1998).
- [10] A. Garuccio, Phys. Rev. A 52, 2535 (1995).
- [11] M. Genovese, G. Brida, C. Novero and E. Predazzi, proceeding of ICSSUR, Napoli may 1999.
- [12] L. Hardy, Phys. Lett. A 161, 326 (1992).
- [13] G. Brida, M. Genovese and C. Novero quant-ph 9911032 and ref.s therein.
- [14] P.G. Kwiat et al., Phys. Rev. A 60 (1999) R773.

Figure caption

Sketch of the source of polarisation entangled photons. CR1 and CR2 are two $LiIO_3$ crystals cut at the phase-matching angle of 51° . L1 and L2 are two identical piano-convex lenses with a hole of 4 mm in the centre. P is a 5 x 5 x 5 mm quartz plate for birefringence compensation and $\Lambda/2$ is a first order half wave-length plate at 351 nm. U.V. identifies the pumping radiation at 351 nm. The infrared beam (I.R.) at 789 nm is generated by a diode laser and is used for system alignment only. The parametric amplifier scheme, described in the text, is shown as well. The dashed line identifies the idler radiation at 633 nm. A second half-wave plate on the I.R. beam (not shown in the figure) allows amplified idler emission from the second crystals too. The figure is not in scale.